

## H. Geometry

### The First (and easiest) Transformation: Translations

Translations	
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**Example 1:** Use the translation  $(x, y) \rightarrow (x-5, y+8)$ .

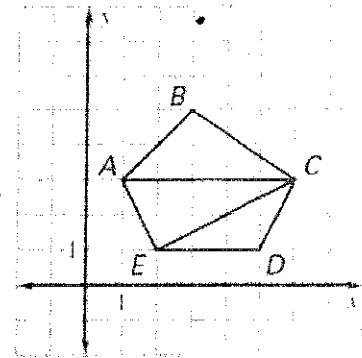
1. What is the image of  $B(4, 2)$ ?
2. What is the image of  $D(21, 5)$ ?
3. What is the preimage of  $F'(23, 24)$ ?
4. What is the preimage of  $H'(7, 25)$ ?
5. What is the image of  $J(0, 2)$ ?
6. What is the preimage of  $K'(24, 6)$ ?

**Example 2:** Instead of writing a "rule" like  $(x+2, y-5)$  many times we just use what is called a vector.

A vector is just the direction you would like the translation to go.

So  $(x+2, y-5)$  would be  $\langle 2, -5 \rangle$  as a vector.

- a) Translate the  $\triangle ABC$  using the vector  $\langle 2, 3 \rangle$ . What are the coordinates of the image?  $A'$  \_\_\_\_\_  $B'$  \_\_\_\_\_  $C'$  \_\_\_\_\_
- b) What is the area of triangle  $ABC$  \_\_\_\_\_
- c) What is the area of triangle  $A'B'C'$  \_\_\_\_\_
- d) What property about translations does part b and c reinforce?



**Example 3: Practice writing and using vectors.**

Given the preimage: Write the image using the translation rule:

$A(2,8)$

$B(5,-3)$

$C(-4,7)$

a)  $(x,y) \rightarrow (x+2,y)$    b)  $(x,y) \rightarrow (x-3,y+3)$    c)  $(x,y) \rightarrow (x-1,y+4)$

Vector \_\_\_\_\_

Vector \_\_\_\_\_

Vector \_\_\_\_\_

Image \_\_\_\_\_

Image \_\_\_\_\_

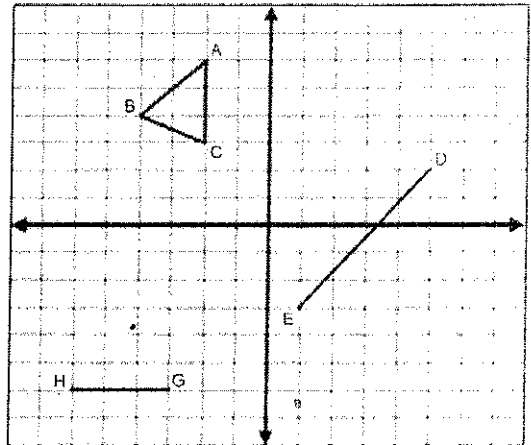
Image \_\_\_\_\_

**Example 4 : Translate  $\triangle ABC$  3 units left and 2 units down.**

1) Rule?  $(x,y) \rightarrow \langle \quad , \quad \rangle$

Pre image:

Image:



Translate  $\overline{ED}$ : 5 units right and 6 units up.  
down.

Translate  $\overline{GH}$ : 7 units left and 9 units down.

# H. Geometry

## The First (and easiest) Transformation: Translations

Translations	<p>Moving or sliding a figure</p> <ul style="list-style-type: none"> <li>- All move the <u>distance</u> and <u>direction</u></li> <li>• Isometry / Rigid motion</li> </ul>
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Example 1: Use the translation  $(x, y) \rightarrow (x-5, y+8)$ .

1. What is the image of  $B(4, 2)$ ?

$$B'(-1, 10)$$

2. What is the image of  $D(21, 5)$ ?

$$D'(16, 13)$$

3. What is the preimage of  $F'(23, 24)$ ?

$$F(28, 16)$$

4. What is the preimage of  $H'(7, 25)$ ?

$$H(13, 17)$$

5. What is the image of  $J(0, 2)$ ?

$$J'(-5, 10)$$

6. What is the preimage of  $K'(24, 6)$ ?

$$K(29, -2)$$

Example 2: Instead of writing a "rule" like  $(x+2, y-5)$  many times we just use what is called a vector.

A vector is just the direction you would like the translation to go.

So  $(x+2, y-5)$  would be  $\langle 2, -5 \rangle$  as a vector.

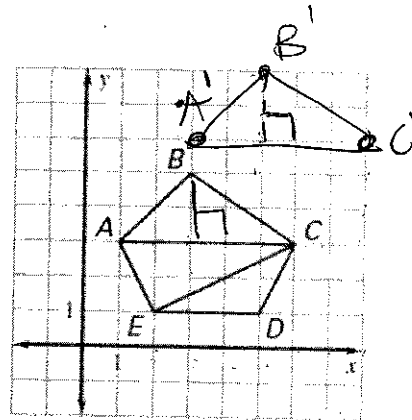
a) Translate the  $\triangle ABC$  using the vector  $\langle 2, 3 \rangle$  What are the coordinates of the image?  $A' (3, 6)$   $B' (5, 0)$   $C' (8, 6)$

b) What is the area of triangle ABC  $5u^2$   $A = \frac{1}{2}bh$

c) What is the area of triangle  $A'B'C'$   $5u^2$

d) What property about translations does part b and c reinforce?

rigid transformation  
isometry



$$b = 5$$

$$h = 2$$

$$A = \frac{1}{2} (5)(2)$$

$$A = 5$$

\*go in reverse

↑  
pay attention to signs

**Example 3: Practice writing and using vectors.**

Given the preimage:

Write the image using the translation rule:

$A(2,8)$

$B(5,-3)$

$C(-4,7)$

a)  $(x,y) \rightarrow (x+2,y)$  b)  $(x,y) \rightarrow (x-3,y+3)$  c)  $(x,y) \rightarrow (x-1,y+4)$

Vector  $\langle 2,0 \rangle$

Vector  $\langle -3,3 \rangle$

Vector  $\langle -1,4 \rangle$

Image  $(4,8)$

Image  $(2,0)$

Image  $(-5,11)$

**Example 4: Translate  $\triangle ABC$  3 units left and 2 units down.**

1) Rule?  $(x,y) \rightarrow \langle -3, -2 \rangle$

Pre image:

Image:

$A(-2,6)$

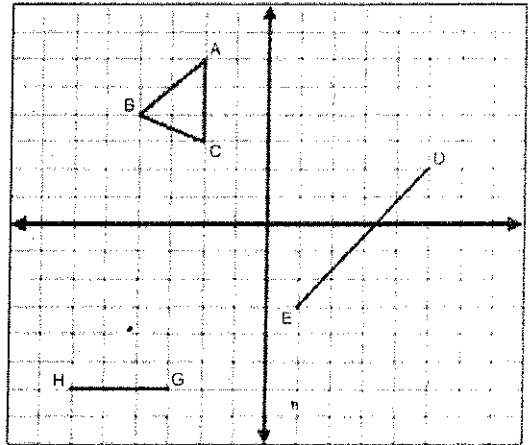
$A'(-5,4)$

$B(-4,4)$

$B'(-7,2)$

$C(-2,3)$

$C'(-5,1)$



Translate  $\overline{ED}$ : 5 units right and 6 units up.  
down.

$E(1,-3) \rightarrow E'(6,3)$

$D(5,2) \rightarrow D'(10,8)$

Translate  $\overline{GH}$ : 7 units left and 9 units

$\langle -7, -9 \rangle$

$G(-3,-6) \rightarrow G'(-10,-15)$

$H(-6,-6) \rightarrow H'(-13,-15)$