

Properties.

1. How can you prove sides or diagonals are congruent in a coordinate plane? distance
2. How can you prove that sides are parallel in a coordinate plane? slope
3. How can you prove that diagonals bisect in a coordinate plane? ~~Midpoint~~ Midpoint
4. How can you prove that diagonals are perpendicular in a coordinate plane? slope

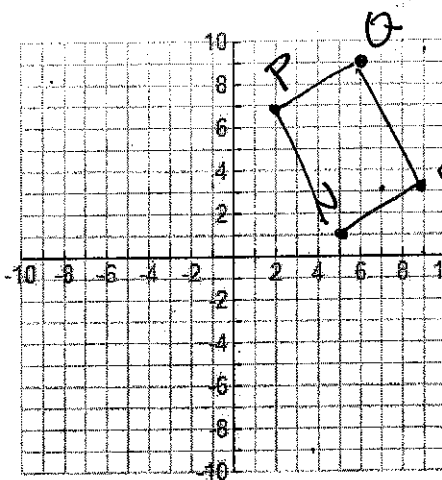
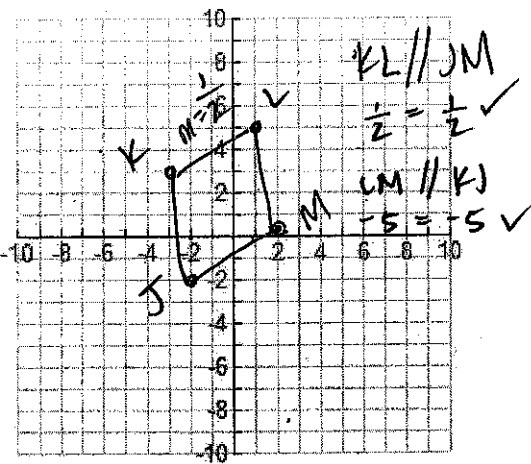
Show that the quadrilateral with the given vertices is a parallelogram using the given definition or theorem.

5. J (-2, -2), K (-3, 3), L (1, 5), M (2, 0)

6. N (5, 1), P (2, 7), Q (6, 9), R (9, 3)

Both pairs of opposite sides are parallel.

Both pairs of opposite sides are congruent.

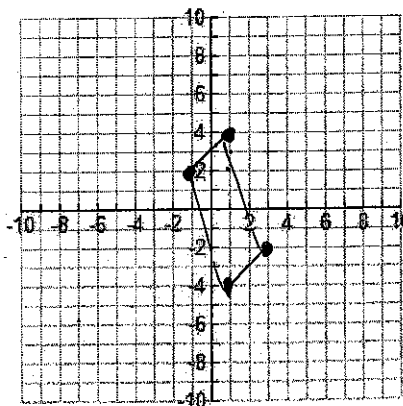
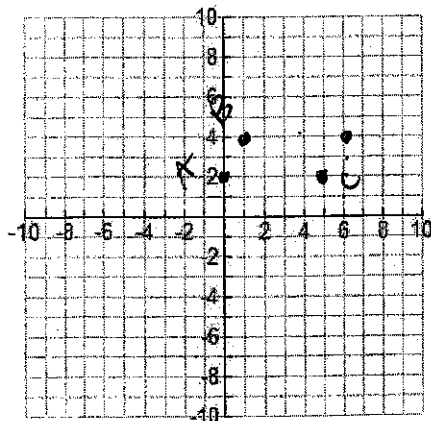


Handwritten notes for quadrilateral NPQR:
 $\overline{PQ} \cong \overline{NR}$
 AND
 $\overline{QR} \cong \overline{PN}$
 $d = \sqrt{(9-7)^2 + (6-2)^2} = \sqrt{20} \checkmark$
 $d = \sqrt{(3-1)^2 + (9-5)^2} = \sqrt{20} \checkmark$
 $d = \sqrt{(3-9)^2 + (9-6)^2} = \sqrt{45} \checkmark$
 $d = \sqrt{(7-1)^2 + (2-5)^2} = \sqrt{45} \checkmark$

Use the given points of parallelogram ABCD to find the missing point of the parallelogram.

7. A (0, 2), B(1, 4), C (5, 2), D (?, ?)

8. A (?, ?), B (1, 4), C (3, -2), D (1, -4)



Handwritten note: $A(-1, 2)$

Handwritten note: $D(6, 4)$

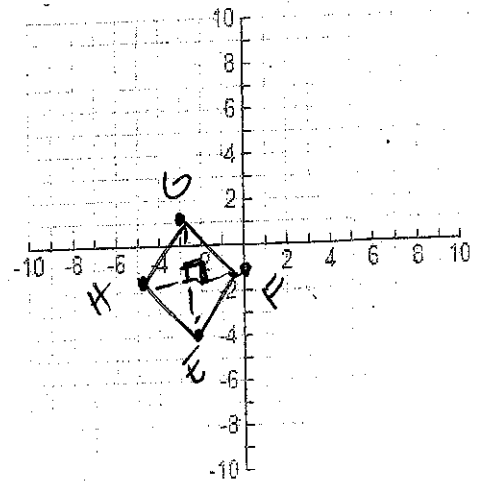
Find the lengths and slopes of the diagonals to determine whether a parallelogram with the given vertices is a rectangle, rhombus, or square.

9. E (-2, -4), F (0, -1), G (-3, 1), H (-5, -2)

EG = $\sqrt{26}$ FH = $\sqrt{13}$

Slope of \overline{EG} = -5 slope of \overline{FH} = $\frac{1}{5}$

Special parallelogram: Rhombus



$d = \sqrt{(1+4)^2 + (-3+2)^2} = \sqrt{26}$

$m = \frac{1+4}{-3+2} = \frac{5}{-1}$

$d = \sqrt{(-2+4)^2 + (-5+2)^2} = \sqrt{13}$

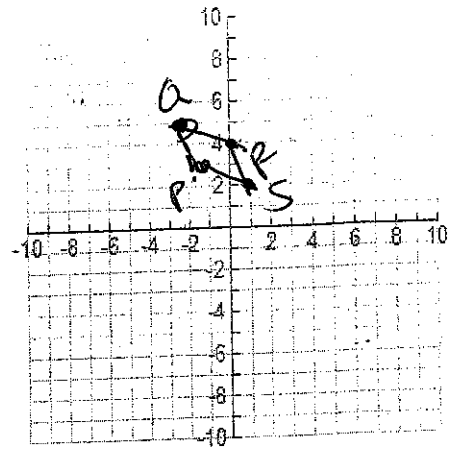
$m = \frac{-2+4}{-5+2} = \frac{-1}{-5} = \frac{1}{5}$

10. P (-1, 3), Q (-2, 5), R (0, 4), S (1, 2)

PR = $\sqrt{2}$ QS = $4\sqrt{2}$

Slope of \overline{PR} = 1 slope of \overline{QS} = -1

Special parallelogram: Rhombus



$d = \sqrt{(4-3)^2 + (0+1)^2} = \sqrt{2}$ $m = \frac{4-3}{0+1} = \frac{1}{1}$

$d = \sqrt{(2+2)^2 + (1-5)^2} = \sqrt{32} = 4\sqrt{2}$ $m = \frac{2-5}{1+2} = \frac{-3}{3}$

1. Triangle DAN has coordinates D(-10, 4), A(-4, 1), and N(-2, 5). Using coordinate geometry, prove that triangle DAN is a right triangle.

$DA = \sqrt{(4-1)^2 + (-10+4)^2} = \sqrt{45}$
 $AN = \sqrt{(5-1)^2 + (-2+4)^2} = \sqrt{20}$
 $DN = \sqrt{(4-5)^2 + (-10+2)^2} = \sqrt{65}$
 $45 + 20 = 65$ ✓

