

Adding and Subtracting Radicals

Example 1:

Evaluate:

a.) $\sqrt{3} + 2\sqrt{3}$

Since these terms are like terms, we simply add.

$$\sqrt{3} + 2\sqrt{3} = 3\sqrt{3}$$

b.) $4\sqrt{2} + \sqrt{8}$

Since these terms are **NOT** like terms, we cannot combine them. We need to simplify each term completely to make sure they can't be written as like terms. If they can, then we will add!

$$\begin{aligned} 4\sqrt{2} + \sqrt{8} &= 4\sqrt{2} + \sqrt{4 \cdot 2} \\ &= 4\sqrt{2} + \sqrt{4} \cdot \sqrt{2} \\ &= 4\sqrt{2} + 2\sqrt{2} \end{aligned}$$

Now they are like terms!

$$= 6\sqrt{2}$$

c.) $5\sqrt{7} - 2\sqrt{28} + 6\sqrt{63}$

d.) $2\sqrt{125x^2z} + 8x\sqrt{80z}$

Adding and Subtracting Radicals

Practice Problems

Evaluate

1. $\underline{4\sqrt{5} + \sqrt{5} - 2\sqrt{5}}$

$$\underline{5\sqrt{5} - 2\sqrt{5}}$$

$$\boxed{3\sqrt{5}}$$

2. $3\sqrt{2} - \sqrt{12}$

$$4 \cdot 3$$

$$\boxed{3\sqrt{2} - 2\sqrt{3}}$$

3. $\sqrt{2x^2} + 3x\sqrt{50} - 25 \cdot 2$

$$x\sqrt{2} + 15x\sqrt{2}$$

$$\boxed{16x\sqrt{2}}$$

4. $\sqrt{20x^2} - 3x\sqrt{5}$

$$4 \cdot 5$$

$$2x\sqrt{5} - 3x\sqrt{5}$$

$$\boxed{-x\sqrt{5}}$$

More Practice with Adding & Subtracting Radicals

Name _____ Date _____

Simplify completely.

1. $\underline{3\sqrt{6}} - \sqrt{3} - \underline{\sqrt{6}} - \underline{2\sqrt{6}}$

$3\sqrt{6} - \sqrt{6} - 2\sqrt{6} - \sqrt{3}$
 ~~$2\sqrt{6} - 2\sqrt{6} - \sqrt{3}$~~
 $(-\sqrt{3})$

3. $\underline{2\sqrt{3}} - \sqrt{3} - 2\sqrt{2} + 2\sqrt{3}$

$\sqrt{3} + 2\sqrt{3} - 2\sqrt{2}$
 $(3\sqrt{3} - 2\sqrt{2})$

2. $-2\sqrt{5} - \sqrt{2} - \sqrt{5} + 2\sqrt{6}$

$-2\sqrt{5} - \sqrt{5} - \sqrt{2} + 2\sqrt{6}$

$(-3\sqrt{5} - \sqrt{2} + 2\sqrt{6})$

4. $\underline{2\sqrt{3}} - 2\sqrt{5} + \underline{3\sqrt{3}} + 3\sqrt{5}$

$(5\sqrt{3} + \sqrt{5})$

5. $2\sqrt{6} - \sqrt{3} + \underline{2\sqrt{6}} - \underline{2\sqrt{6}}$

$2\sqrt{6} - \sqrt{3}$

6. $-2\sqrt{12} + 2\sqrt{3} + 3\sqrt{45}$
 $4 \cdot 3 \qquad 9 \cdot 5$

$-4\sqrt{3} + 2\sqrt{3} + 9\sqrt{5}$

$(-2\sqrt{3} + 9\sqrt{5})$

7. $-\sqrt{45} + 2\sqrt{27} + 2\sqrt{5}$
 $9 \cdot 5 \qquad 9 \cdot 3$

$-3\sqrt{5} + 6\sqrt{3} + 2\sqrt{5}$
 $(-\sqrt{5} + 6\sqrt{3})$

8. $-2\sqrt{6} - \sqrt{54} + 2\sqrt{24}$
 $9 \cdot 6 \qquad 4 \cdot 6$

$-2\sqrt{6} - 3\sqrt{6} + 4\sqrt{6}$
 $(-\sqrt{6})$

$$9. -2\sqrt{5} + 3\sqrt{8} - 3\sqrt{18}$$

$\begin{matrix} \curvearrowright & \curvearrowright \\ 4 \cdot 2 & 9 \cdot 2 \end{matrix}$

$$-2\sqrt{5} + 6\sqrt{2} - 9\sqrt{2}$$

$$\underline{-2\sqrt{5} - 3\sqrt{2}}$$

$$10. 3\sqrt{45} - 2\sqrt{54} + 2\sqrt{6}$$

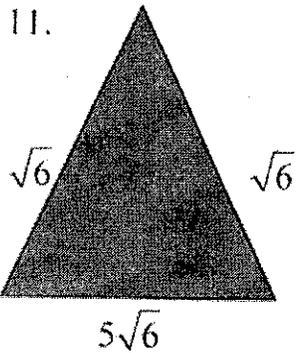
$\begin{matrix} \curvearrowright & \curvearrowright \\ 9 \cdot 5 & 9 \cdot 6 \end{matrix}$

$$9\sqrt{5} - 6\sqrt{6} + 2\sqrt{6}$$

$$\underline{9\sqrt{5} - 4\sqrt{6}}$$

Find the perimeter of the following figures.

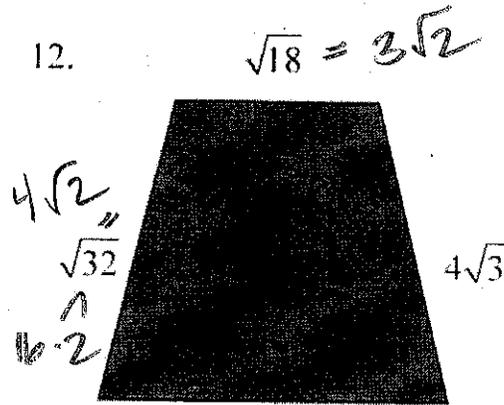
11.



$$P = \sqrt{6} + \sqrt{6} + 5\sqrt{6}$$

$$\underline{P = 7\sqrt{6}}$$

12.



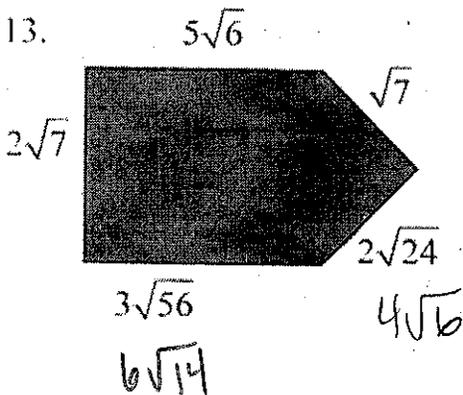
$$2\sqrt{45} = 6\sqrt{5}$$

\uparrow
9 · 5

$$P = 3\sqrt{2} + 4\sqrt{2} + 6\sqrt{5} + 4\sqrt{3}$$

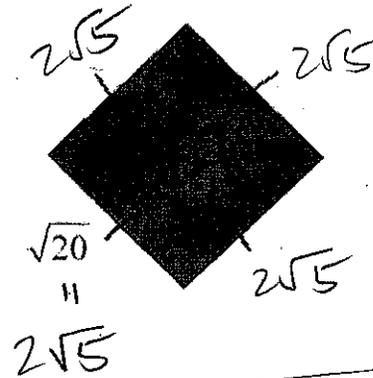
$$\underline{P = 7\sqrt{2} + 6\sqrt{5} + 4\sqrt{3}}$$

13.



$$\underline{P = 6\sqrt{14} + 9\sqrt{6} + 3\sqrt{7}}$$

14.



$$\boxed{P = 8\sqrt{5}}$$