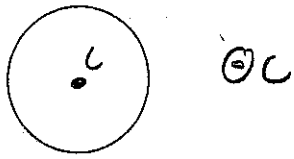
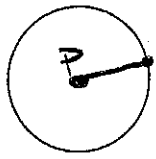
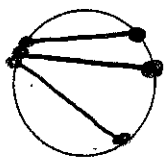
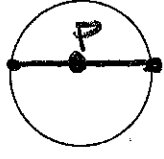
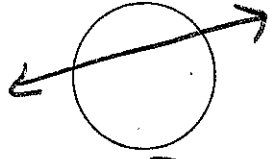
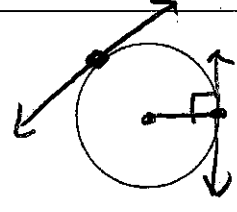
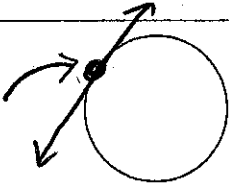


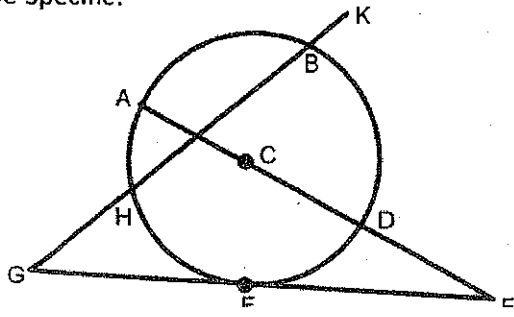
Unit 8: Properties of Circles

Circle Vocabulary and Tangents

Objective: Identify segments and lines related to circles.
Use properties of a tangent to a circle.

Word	Description	Drawing
Circle:	set of all pts equidistant from a given point called the center	
Radius:	Distance from center to point on the circle	
Chord:	A segment whose endpoints are on the circle	
Diameter:	Distance across circle through center - longest chord	
Secant:	Intersects the circle at exactly two points	
Tangent:	- Intersects the circle at exactly one point - forms 90° with radius	
Point of Tangency:	Point where the tangent intersects circle	

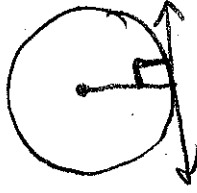
EXAMPLE 1: Tell whether the line or segment is best described as a chord, a secant, a tangent, a diameter, or a radius—be specific!



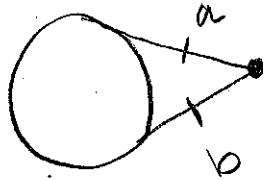
- a. \overline{AD} Diameter
- b. \overline{CD} radius
- c. \overline{EG} Tangent
- d. \overline{HB} Chord
- e. \overline{FB} None
- f. \overline{FE} tangent

RULE:

In a plane, a line is tangent to a circle if and only if the line is perpendicular to a radius of the circle at its endpoint on the circle

**RULE:**

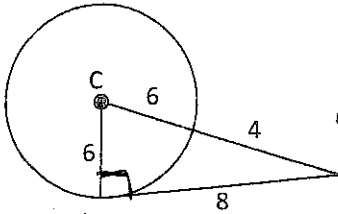
Tangent segments from a common external point are congruent.



$$a = b$$

EXAMPLE 2: Verifying a Tangent to a Circle. (Use the Pythagorean Theorem Converse!)

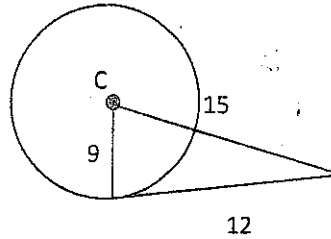
a.



$$6^2 + 8^2 = 10^2$$

$$100 = 100 \checkmark$$

b.

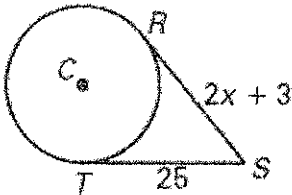


$$9^2 + 12^2 = 15^2$$

$$225 = 225 \checkmark$$

EXAMPLE 3: Using Properties of Tangents \overline{SR} and \overline{ST} are tangent to $\odot C$. Find the value of x .

a.

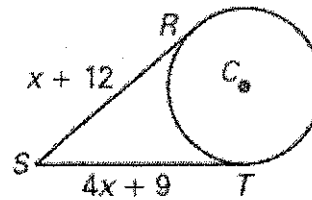


$$2x + 3 = 25$$

$$2x = 22$$

$$\boxed{x = 11}$$

b.



$$x + 12 = 4x + 9$$

$$3 = 3x$$

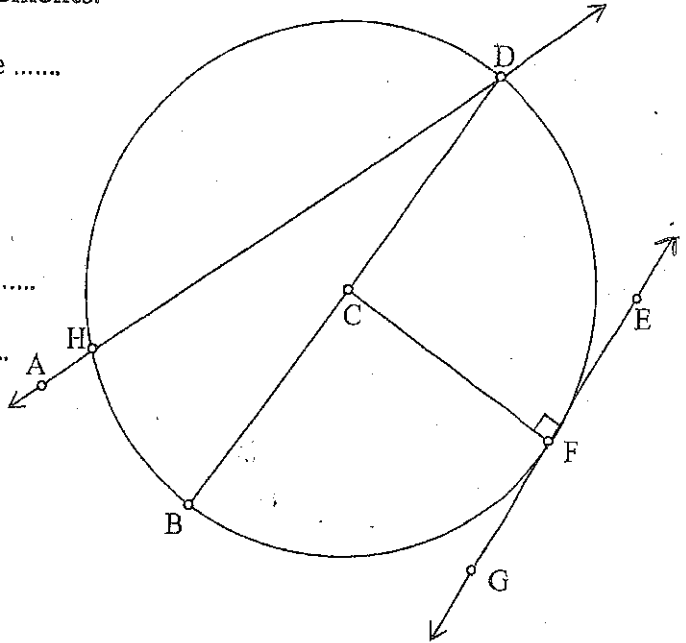
$$\boxed{x = 1}$$

Worksheet - 11.1

Lines that Intersect Circles

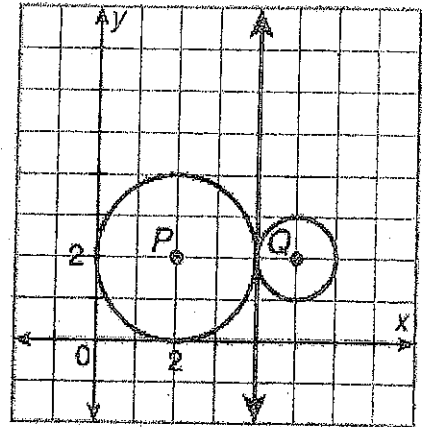
Use the figure below to complete the following statements.

- | | |
|--------------|--|
| 1) <u>CF</u> | 1. Three radii of the circle are |
| <u>CD</u> | |
| <u>CB</u> | |
| 2) <u>BD</u> | 2. A diameter of the circle is |
| 3) <u>GE</u> | 3. A tangent of the circle is |
| 4) <u>HD</u> | 4. A chord of the circle is |
| 5) <u>AD</u> | 5. A secant of the circle is |
| 6) <u>F</u> | 6. A point of tangency is |



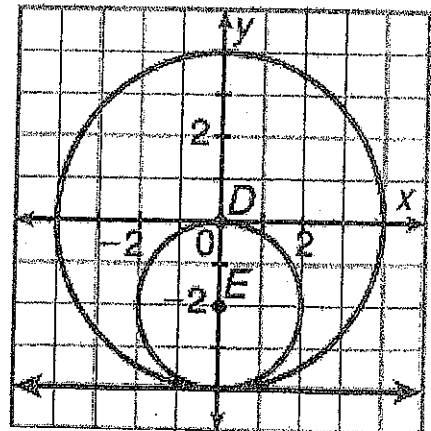
Use the figure below to answer the exercise #7-10.

- | | |
|------------------|---|
| 7) <u>2</u> | 7. Radius of $\odot P$ |
| 8) <u>1</u> | 8. Radius of $\odot Q$ |
| 9) <u>(4, 2)</u> | 9. Coordinates of the point of tangency |
| 10) <u>X=4</u> | 10. Equation of the tangent line at the point of tangency |



Use the figure below to answer the exercise #11-14.

- | | |
|--------------------|---|
| 11) <u>4</u> | 11. Radius of $\odot D$ |
| 12) <u>2</u> | 12. Radius of $\odot E$ |
| 13) <u>(0, -4)</u> | 13. Coordinates of the point of tangency |
| 14) <u>y = -4</u> | 14. Equation of the tangent line at the point of tangency |



Fill in the blanks to complete each theorem.

15) tangent

15. If a line is perpendicular to a radius of a circle at a point on a circle, then the line is ? to the circle.

16) Congruent

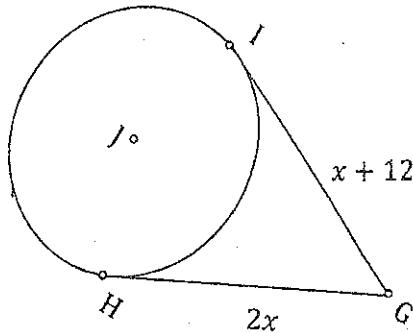
16. If two segments are tangent to a circle from the same external point, then the segments are ?.

17) perpendicular

17. If a line is tangent to a circle, then it is ? to the radius drawn to the point of tangency.

In exercises #18 - 21, \overline{GH} and \overline{GI} are tangents to $\odot J$. Find GH .

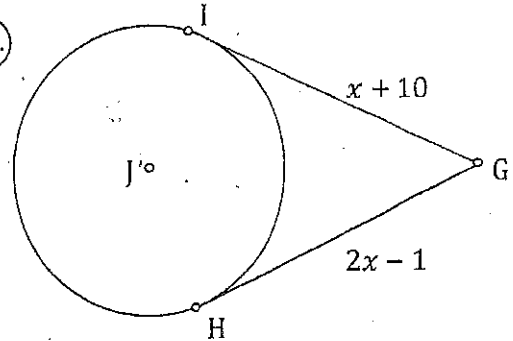
18) 12 (21) (18)



$$2x = x + 12$$

$$x = 12$$

(19)

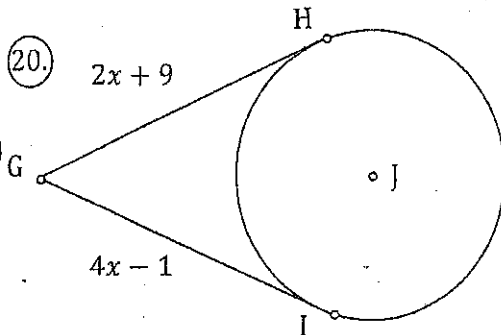


$$x + 10 = 2x - 1$$

$$11 = x$$

19) 11 (21)

20) 5 (19) (20)

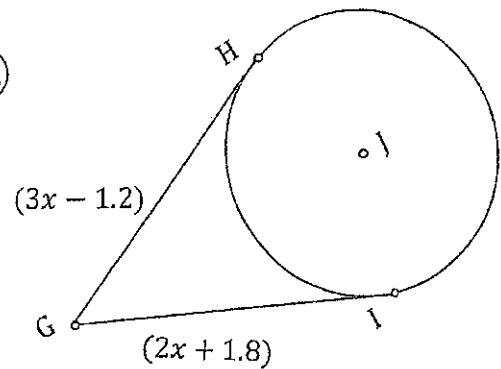


$$2x + 9 = 4x - 1$$

$$10 = 2x$$

$$x = 5$$

(21)



$$3x - 1.2 = 2x + 1.8$$

$$x = 3$$

21) 3 (7.8)